End-to-End Training of Deep Visuomotor Policies

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Content

- Related work
- Method
- **•** Experiments
- Discussions

Model-based Reinforcement Learning

What is "model-based RL"?

What is a "model"?

How does it differ from model-free RL?

Model-free vs. model-based reinforcement learning

Collect data

$$
\mathcal{D} = \{s_t, a_t, r_{t+1}, s_{t+1}\}_{t=0}^T
$$

Model-free: learn policy directly from data

$$
\mathcal{D} \rightarrow \pi
$$
 e.g. Q-learning, policy gradient

Model-based: learn model, then use it to learn or improve a policy

$$
\mathcal{D}\to f\to\pi
$$

Reference: https://docs.google.com/presentation/d/1f-DIrIvh44-jmTIKdKcue0Hx2RqQSw52t4k8HEdn5-c/edit#slide=id.g81ed7b35e4_0_2038

What is a model?

Definition: a model is a representation that **explicitly** encodes knowledge about the structure of the environment and task.

- A transition/dynamics model: $s_{t+1} = f_s(s_t, a_t)$
- A model of rewards: $r_{t+1} = f_r(s_t, a_t)$

Typically what is meant by the model in model-based RL

• An inverse transition/dynamics model: $a_t = f_s^{-1}(s_t, s_{t+1})$

• A model of distance:
$$
d_{ij} = f_d(s_i, s_j)
$$

• A model of future returns: $G_t = Q(s_t, a_t)$ or $G_t = V(s_t)$

Reference: https://docs.google.com/presentation/d/1f-DIrIvh44-jmTIKdKcue0Hx2RqQSw52t4k8HEdn5-c/edit#slide=id.g81ed7b35e4_0_2038

Learning Perception and Control Policy Separately

● Separated vision pipeline and robot control pipeline

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Example: Learning "Ball-in-the-Cup"

A stereo vision system was used to track the position of the ball. This ball position was used for determining the reward.

[1] Deisenroth, Marc Peter, Gerhard Neumann, and Jan Peters. "A survey on policy search for robotics." Foundations and Trends® in Robotics 2.1–2 (2013): 1-142. [2] J. Kober and J. Peters. "Policy Search for Motor Primitives in Robotics." Machine Learning, pages 1–33, 2010.

Learning Perception and Control Policy Separately

Benefit:

- Avoid hand-crafted design of visual perception model
- Perception gets better with policy training

High-dimensional RGB input \rightarrow Deep neural networks!

- High-dimensional RGB input \rightarrow Deep neural networks!
- But …
	- Needs a lot of training data
	- Needs supervision of "ground-truth" actions

Related work

- **● Application of deep learning on robotics control**
	- **○ Backpropagation: non-differentiable and instable**
	- **○ Not sample-efficient (unrealistic in real-world scene)**

• What is trajectory optimization method?

$$
\min_{u_1,\dots,u_t} \sum_{t=1}^T c(x_t,u_t) \text{ s.t. } x_t = f(x_{t-1},u_{t-1})
$$

 u_t is the action at time step t

 x_t is the state at time step t

 f is the transition function

 c is the cost function (negative reward of RL problem)

joint angles, end-effector pose, object positions, and their velocities; dimensionality: 14 to 32

- The controller learns a sequence of actions (trajectory) given fully observed state
- But it cannot generalize!
- In contrast, a policy can generalize better

• Trajectory Optimization Method \rightarrow Guided Policy Search

$$
\min_{u_1,\ldots,u_t} \sum_{t=1}^T c(x_t,u_t) \text{ s.t. } x_t = f(x_{t-1},u_{t-1}) \ \ \boldsymbol{\longrightarrow} \ \min_{\tau} c(\overset{\textstyle\overline{\rightthreetimes}}{\tau})
$$

a sequence of actions (trajectory)

 u_t is the action at time step t x_t is the state at time step t f is the transition function c is the cost function (negative reward of RL problem)

Credit: https://michaelrzhang.github.io/model-based-rl

• Trajectory Optimization Method \rightarrow Guided Policy Search

$$
\min_{u_1,\ldots,u_t} \sum_{t=1}^T c(x_t,u_t) \text{ s.t. } x_t = f(x_{t-1},u_{t-1}) \qquad \qquad \min_\tau c(\tau)
$$

 u_t is the action at time step t x_t is the state at time step t f is the transition function c is the cost function (negative reward of RL problem)

• Trajectory Optimization Method \rightarrow Guided Policy Search

$$
\min_{u_1,\ldots,u_t} \sum_{t=1}^T c(x_t,u_t) \text{ s.t. } x_t = f(x_{t-1},u_{t-1}) \qquad \qquad \min_\tau c(\tau)
$$

 u_t is the action at time step t x_t is the state at time step t f is the transition function c is the cost function (negative reward of RL problem)

$$
\min_{\tau,\theta} c(\tau) \text{ s.t. } u_t = \pi_{\theta}(x_t) \Big\downarrow \text{Lagrangian} \mathcal{L}(\tau,\theta,\lambda) = c(\tau) + \sum_{t=1}^T \lambda_t (\pi_{\theta}(x_t) - u_t)
$$

● Guided Policy Search - Optimization

$$
\mathcal{L}(\tau, \theta, \lambda) = c(\tau) + \sum_{t=1}^T \lambda_t (\pi_\theta(x_t) - u_t)
$$

Standard optimization problem Solve it using ADMM

1. Start with some initial choice of λ (by λ , we include λ_t corresponding to each time step) 2. Assign $\tau \leftarrow \arg \min_{\tau} \mathcal{L}(\tau, \theta, \lambda)$. 3. Assign $\theta \leftarrow \arg \min_{\theta} \mathcal{L}(\tau, \theta, \lambda)$. 4. Compute $\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\tau, \theta, \lambda)$. Take a gradient step $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$ 5. Repeat steps 2-4.

● Guided Policy Search - Optimization

$$
\mathcal{L}(\tau, \theta, \lambda) = c(\tau) + \sum_{t=1}^T \lambda_t (\pi_\theta(x_t) - u_t)
$$

Standard optimization problem Solve it using ADMM

1. Start with some initial choice of λ (by λ , we include λ_t corresponding to each time step) Use some trajectory optimization methods to solve it 2. Assign $\tau \leftarrow \arg \min_{\tau} \mathcal{L}(\tau, \theta, \lambda)$. 3. Assign $\theta \leftarrow \arg \min_{\theta} \mathcal{L}(\tau, \theta, \lambda)$. 4. Compute $\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\tau, \theta, \lambda)$. Take a gradient step $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$ 5. Repeat steps 2-4.

● Guided Policy Search - Optimization

$$
\mathcal{L}(\tau, \theta, \lambda) = c(\tau) + \sum_{t=1}^T \lambda_t (\pi_\theta(x_t) - u_t)
$$

Standard optimization problem Solve it using ADMM

1. Start with some initial choice of λ (by λ , we include λ_t

corresponding to each time step)
\n2. Assign
$$
\tau \leftarrow \arg \min_{\tau} \mathcal{L}(\tau, \theta, \lambda)
$$
.
\n3. Assign $\theta \leftarrow \arg \min_{\theta} \mathcal{L}(\tau, \theta, \lambda)$.
\n4. Compute $\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\tau, \theta, \lambda)$. Take a gradient step
\n $\lambda \leftarrow \lambda + \alpha \frac{dg}{d\lambda}$
\n5. Repeat steps 2-4.

Guided Policy Search

$$
\mathcal{L}(\tau, \theta, \lambda) = c(\tau) + \sum_{t=1}^T \lambda_t (\pi_\theta(x_t) - u_t)
$$

1. Start with some initial choice of λ (by λ , we include λ_t corresponding to each time step)

2. Assign $\tau \leftarrow \arg \min_{\tau} \mathcal{L}(\tau, \theta, \lambda)$.

3. Assign $\theta \leftarrow \arg \min_{\theta} \mathcal{L}(\tau, \theta, \lambda)$.

4. Compute $\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\tau, \theta, \lambda)$. Take a gradient step $\frac{1}{\sqrt{1-\frac{1}{2}}}$

$$
\lambda \leftarrow \lambda + \alpha \frac{d\lambda}{d\lambda}
$$

5. Repeat steps 2-4.

Recap:

- Each trajectory-centric teacher only needs to solve the task from a single initial state \rightarrow make the problem easier
- The policy is trained with supervised learning \rightarrow good generalization
- Iterative adaptation of teacher trajectories & final policy \rightarrow the teacher does not take actions that the final policy cannot reproduce

Visuomotor Policy Architecture

$$
s_{cij}\,=\,e^{a_{cij}}/\textstyle\sum_{i'j'}\,e^{a_{ci'j'}}
$$

$$
f_{cx} = \sum_{ij} s_{cij} x_{ij}
$$

$$
f_{cy} = \sum_{ij} s_{cij} y_{ij}
$$

- Spatial softmax \rightarrow soft version of max pooling
- Get the feature points
- Learns the spatial information better

Training procedural

- **○ Pretraining convolutional layers**
- **○ Pretraining local controller**
- **○ End-to-end guided policy search**

Method

● Algorithm

Target:

$$
\min_{p,\pi_{\theta}} E_p[\ell(\tau)] \text{ s.t. } p(\mathbf{u}_t|\mathbf{x}_t) = \pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t) \ \forall \mathbf{x}_t, \mathbf{u}_t, t,
$$

$$
\ell(\tau) = \textstyle\sum_{t=1}^T \ell(\mathbf{x}_t,\mathbf{u}_t)
$$

$$
\min_{p,\pi_{\theta}} E_{p}[\ell(\tau)] \text{ s.t. } p(\mathbf{u}_{t}|\mathbf{x}_{t}) = \pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t}) \forall \mathbf{x}_{t}, \mathbf{u}_{t}, t,
$$
\nMethod

\n
$$
\ell(\tau) = \sum_{t=1}^{T} \ell(\mathbf{x}_{t}, \mathbf{u}_{t}) \quad \underset{1}{\begin{subarray}{c}\text{min}_{\mathbf{x} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m}}} f(\mathbf{x}) + g(\mathbf{z}) \\
\vdots \\
\underset{1}{\begin{subarray}{c}\text{min}_{\mathbf{y} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m}}} \end{subarray}} f(\mathbf{x}) + g(\mathbf{z}) \\
\vdots \\
\underset{1}{\begin{subarray}{c}\text{min}_{\mathbf{y} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m}}} \end{subarray}} f(\mathbf{x}) + g(\mathbf{z}) \\
\vdots \\
\underset{1}{\begin{subarray}{c}\text{min}_{\mathbf{y} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m}}} \end{subarray}} f(\mathbf{x}) + g(\mathbf{z}) \\
\vdots \\
\underset{1}{\begin{subarray}{c}\text{min}{\mathbf{y} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m}}} \end{subarray}} f(\mathbf{x}, \mathbf{u}_{t}) + E_{p(\mathbf{x}_{t}, \mathbf{u}_{t})}[\ell(\mathbf{x}_{t}, \mathbf{u}_{t})] + E_{p(\mathbf{x}_{t}, \mathbf{y}_{t} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m}}] \cdot [\mathbf{x}_{t}, \mathbf{u}_{t}) + \nu_{t} \phi_{t}^{\theta}(\theta, p)} \\
\downarrow \\
\underset{1}{\begin{subarray}{c}\text{minimization step for } \mathbf{x} \in \mathbb{R}^{m}, \mathbf{z} \in \mathbb{R}^{m} \end{subarray}} f(\mathbf{x}_{t}, \mathbf{u}_{t}) + E_{p(\mathbf{x}_{t}, \mathbf{u}_{t})}[\ell(\mathbf{x}_{t}, \mathbf{u}_{t})] + E_{p(\mathbf{x}_{t}, \
$$

Method

• **Algorithm**
\n
$$
\theta \leftarrow \arg \min_{\theta} \sum_{t=1}^{T} E_{p(\mathbf{x}_t)\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)}[\lambda_{\mathbf{x}_t,\mathbf{u}_t}] + \nu_t \phi_t^{\theta}(\theta, p)
$$
\n
$$
p \leftarrow \arg \min_{p} \sum_{t=1}^{T} E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\ell(\mathbf{x}_t,\mathbf{u}_t) - \lambda_{\mathbf{x}_t,\mathbf{u}_t}] + \nu_t \phi_t^p(p, \theta)
$$
\n
$$
\lambda_{\mathbf{x}_t,\mathbf{u}_t} \leftarrow \lambda_{\mathbf{x}_t,\mathbf{u}_t} + \alpha \nu_t (\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)p(\mathbf{x}_t) - p(\mathbf{u}_t|\mathbf{x}_t)p(\mathbf{x}_t)).
$$
\n
$$
\theta \leftarrow \arg \min_{\theta} \sum_{t=1}^{T} E_{p(\mathbf{x}_t)\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)}[\mathbf{u}_t^{\mathrm{T}}\lambda_{\mu t}] + \nu_t \phi_t^{\theta}(\theta, p)
$$
\n
$$
p \leftarrow \arg \min_{p} \sum_{t=1}^{T} E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\ell(\mathbf{x}_t,\mathbf{u}_t) - \mathbf{u}_t^{\mathrm{T}}\lambda_{\mu t}] + \nu_t \phi_t^p(p, \theta)
$$
\n
$$
\lambda_{\mu t} \leftarrow \lambda_{\mu t} + \alpha \nu_t (E_{\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)p(\mathbf{x}_t)}[\mathbf{u}_t] - E_{p(\mathbf{u}_t|\mathbf{x}_t)p(\mathbf{x}_t)}[\mathbf{u}_t]),
$$

$$
\mathcal{L}_p(p,\theta) = \sum_{t=1}^T E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\ell(\mathbf{x}_t,\mathbf{u}_t)] + E_{p(\mathbf{x}_t)\pi_\theta(\mathbf{u}_t|\mathbf{x}_t)}[\lambda_{\mathbf{x}_t,\mathbf{u}_t}] - E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\lambda_{\mathbf{x}_t,\mathbf{u}_t}] + \nu_t \phi_t^p(\theta,p),
$$

\n
$$
p \leftarrow \arg \min_p \sum_{t=1}^T E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\ell(\mathbf{x}_t,\mathbf{u}_t) - \mathbf{u}_t^{\mathrm{T}}\lambda_{\mu t}] + \nu_t \phi_t^p(p,\theta)
$$

● Trajectory optimization under unknown dynamics

$$
p(\mathbf{u}_t|\mathbf{x}_t) = \mathcal{N}(\mathbf{K}_t\mathbf{x}_t + \mathbf{k}_t, \mathbf{C}_t) \qquad p(\mathbf{x}_{t+1}|\mathbf{x}_t, \mathbf{u}_t) = \mathcal{N}(f_{\mathbf{x}t}\mathbf{x}_t + f_{\mathbf{u}t}\mathbf{u}_t + f_{ct}, \mathbf{F}_t).
$$

$$
\min_{p(\tau)\in\mathcal{N}(\tau)} \mathcal{L}_p(p,\theta) \text{ s.t. } D_{\text{KL}}(p(\tau)\|\hat{p}(\tau)) \leq \epsilon.
$$

$\mathcal{L}_{\theta}(\theta, p) = \sum_{t=1}^{I} E_{p(\mathbf{x}_t, \mathbf{u}_t)} [\ell(\mathbf{x}_t, \mathbf{u}_t)] + E_{p(\mathbf{x}_t)\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)} [\lambda_{\mathbf{x}_t, \mathbf{u}_t}] - E_{p(\mathbf{x}_t, \mathbf{u}_t)} [\lambda_{\mathbf{x}_t, \mathbf{u}_t}] + \nu_t \phi_t^{\theta}(\theta, p) \ \theta \leftarrow \arg \min_{\theta} \sum_{t=1}^{T} E_{p(\mathbf{x}_t)\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)}[\mathbf{u}_$ Method

● Supervised policy optimization

$$
\mathcal{L}_{\theta}(\theta, p) = \frac{1}{2N} \sum_{i=1}^{N} \sum_{t=1}^{T} E_{p_i(\mathbf{x}_t, \mathbf{o}_t)} \left[\text{tr}[\mathbf{C}_{ti}^{-1} \Sigma^{\pi}(\mathbf{o}_t)] - \log |\Sigma^{\pi}(\mathbf{o}_t)| \right] + (\mu^{\pi}(\mathbf{o}_t) - \mu_{ti}^{p}(\mathbf{x}_t)) \mathbf{C}_{ti}^{-1}(\mu^{\pi}(\mathbf{o}_t) - \mu_{ti}^{p}(\mathbf{x}_t)) + 2\lambda_{\mu t}^{T} \mu^{\pi}(\mathbf{o}_t) \right],
$$

$$
\pi_\theta(\mathbf{u}_t|\mathbf{o}_t) = \mathcal{N}(\mu^\pi(\mathbf{o}_t), \Sigma^\pi(\mathbf{o}_t))
$$

- How does the guided policy search algorithm compare to other policy search methods for training complex, high-dimensional policies, such as neural networks?
- Does our trajectory optimization algorithm work on a real robotic platform with unknown dynamics, for a range of different tasks?
- How does our **spatial softmax architecture** compare to other, more standard convolutional neural network architectures?
- Does training the perception and control systems in a visuomotor policy jointly end-to-end provide better performance than training each component separately?

• How does the guided policy search algorithm compare to other policy search methods for training complex, high-dimensional policies, such as neural networks?

- How does the guided policy search algorithm compare to other policy search methods for training complex, high-dimensional policies, such as neural networks?
	- Compare with methods that do not use vision, but use system states
	- GPS is more sample efficient
	- Better generalization in testing

● Does our trajectory optimization algorithm work on a real robotic platform with unknown dynamics, for a range of different tasks?

- Sample efficient (20-25 samples)
- Robustness

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	- Sample efficient (20-25 samples)
	- Robustness

● How does our spatial softmax architecture compare to other, more standard convolutional neural network architectures?

Performance on Object Pose Estimation Pretraining Task

● Visualization of feature points

• Does training the perception and control systems in a visuomotor policy jointly end-to-end provide better performance than training each component separately?

Baselines:

train the vision layers in advance, then train the policy

Success rates on training positions, on novel test positions, and in the presence of visual distractors. The number of trials per test is shown in parentheses.

- What are the drawbacks/limitations for this method?

• Needs Full-state observations during training

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- Dependent on hand-crafted rewards

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- Dependent on hand-crafted rewards
- Relying on the ability of Trajectory Optimization Method (teachers) to discover good trajectories

Questions?