# End-to-End Training of Deep Visuomotor Policies

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# Content

- Related work
- Method
- Experiments
- Discussions

# Model-based Reinforcement Learning

What is "model-based RL"?

What is a "model"?

How does it differ from model-free RL?

#### Model-free vs. model-based reinforcement learning

Collect data

$$\mathcal{D} = \{s_t, a_t, r_{t+1}, s_{t+1}\}_{t=0}^T$$

#### Model-free: learn policy directly from data

$$\mathcal{D} 
ightarrow \pi$$
 e.g. Q-learning, policy gradient

Model-based: learn model, then use it to learn or improve a policy

$$\mathcal{D} \to f \to \pi$$

Reference: https://docs.google.com/presentation/d/1f-DIrlvh44-jmTIKdKcue0Hx2RqQSw52t4k8HEdn5-c/edit#slide=id.g81ed7b35e4\_0\_2038

# What is a model?

Definition: a model is a representation that **explicitly** encodes knowledge about the structure of the environment and task.

- A transition/dynamics model:  $s_{t+1} = f_s(s_t, a_t)$  ,
- A model of rewards:  $r_{t+1} = f_r(s_t, a_t)$

Typically what is meant by the model in model-based RL

• An inverse transition/dynamics model:  $a_t = f_s^{-1}(s_t, s_{t+1})$ 

• A model of distance: 
$$d_{ij} = f_d(s_i,s_j)$$

• A model of future returns:  $G_t = Q(s_t, a_t)$  or  $G_t = V(s_t)$ 

Reference: https://docs.google.com/presentation/d/1f-DIrlvh44-jmTIKdKcue0Hx2RqQSw52t4k8HEdn5-c/edit#slide=id.g81ed7b35e4\_0\_2038

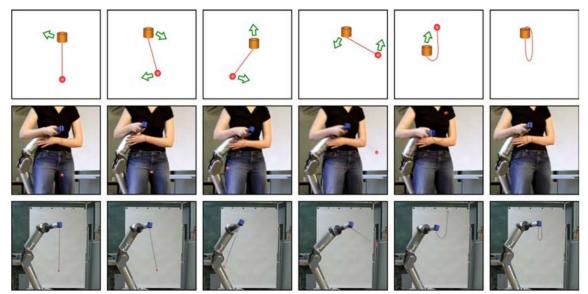
# Learning Perception and Control Policy Separately

• Separated vision pipeline and robot control pipeline

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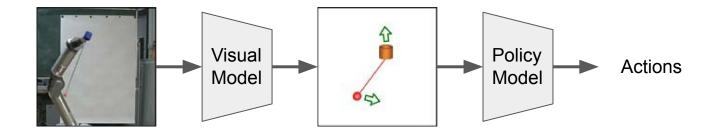
Example: Learning "Ball-in-the-Cup"

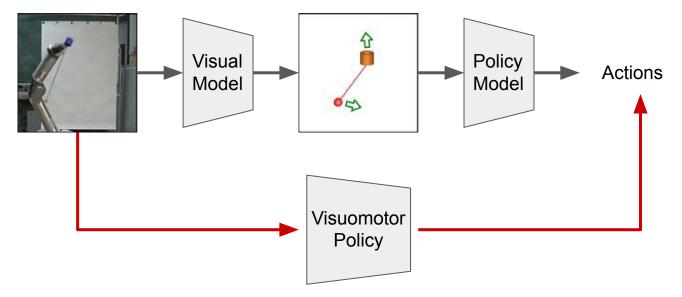


A stereo vision system was used to track the position of the ball. This ball position was used for determining the reward.

[1] Deisenroth, Marc Peter, Gerhard Neumann, and Jan Peters. "A survey on policy search for robotics." Foundations and Trends® in Robotics 2.1–2 (2013): 1-142. [2] J. Kober and J. Peters. "Policy Search for Motor Primitives in Robotics." Machine Learning, pages 1–33, 2010.

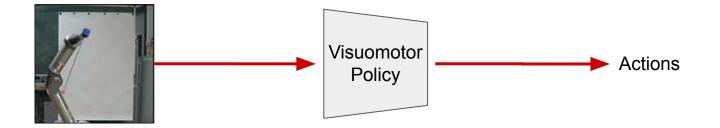
#### Learning Perception and Control Policy Separately



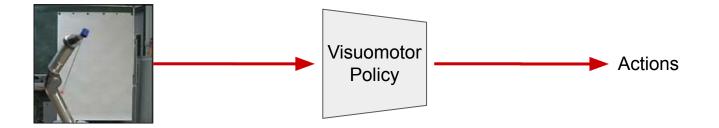


Benefit:

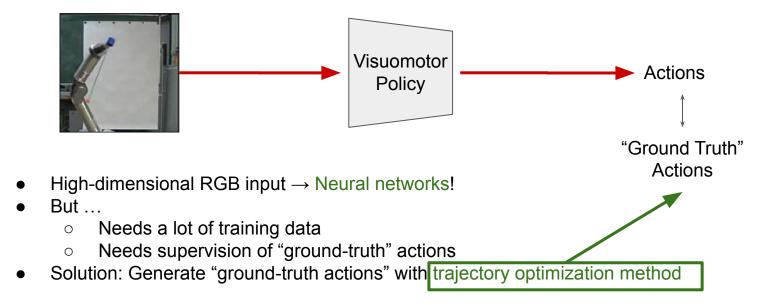
- Avoid hand-crafted design of visual perception model
- Perception gets better with policy training



• High-dimensional RGB input  $\rightarrow$  Deep neural networks!



- High-dimensional RGB input → Deep neural networks!
- But ...
  - Needs a lot of training data
  - Needs supervision of "ground-truth" actions



# **Related work**

- Application of deep learning on robotics control
  - Backpropagation: non-differentiable and instable
  - Not sample-efficient (unrealistic in real-world scene)

What is trajectory optimization method?

$$\min_{u_1,\ldots,u_t} \sum_{t=1}^T c(x_t,u_t) ext{ s.t. } x_t = f(x_{t-1},u_{t-1})$$

 $u_t$  is the action at time step t

 $x_t$  is the state at time step t

 $\boldsymbol{f}$  is the transition function

c is the cost function (negative reward of RL problem)

joint angles, end-effector pose, object positions, and their velocities; dimensionality: 14 to 32

- The controller learns a sequence of actions (trajectory) given fully observed state
- But it cannot generalize!
- In contrast, a policy can generalize better

• Trajectory Optimization Method → Guided Policy Search

$$\min_{u_1,\ldots,u_t}\sum_{t=1}^T c(x_t,u_t) ext{ s.t. } x_t = f(x_{t-1},u_{t-1}) \quad \longrightarrow \quad \min_{ au} c( au)$$

a sequence of actions (trajectory)

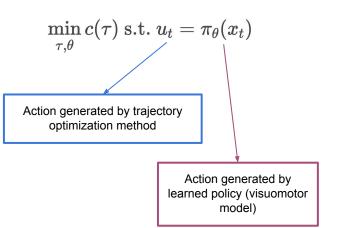
 $u_t$  is the action at time step t  $x_t$  is the state at time step t f is the transition function c is the cost function (negative reward of RL problem)

Credit: https://michaelrzhang.github.io/model-based-rl

• Trajectory Optimization Method  $\rightarrow$  Guided Policy Search

$$\min_{u_1,\ldots,u_t}\sum_{t=1}^T c(x_t,u_t) ext{ s.t. } x_t = f(x_{t-1},u_{t-1}) \qquad \quad \min_ au c( au)$$

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 $u_t$  is the action at time step t  $x_t$  is the state at time step t f is the transition function c is the cost function (negative reward of RL problem)

$$egin{aligned} \min_{ au, heta} c( au) ext{ s.t. } u_t &= \pi_ heta(x_t) \ & igcap_{ ext{Lagrangian}} \ \mathcal{L}( au, heta,\lambda) &= c( au) + \sum_{t=1}^T \lambda_t(\pi_ heta(x_t) - u_t) \end{aligned}$$

Guided Policy Search - Optimization

$$\mathcal{L}( au, heta,\lambda)=c( au)+\sum_{t=1}^T\lambda_t(\pi_ heta(x_t)-u_t)$$

Standard optimization problem Solve it using ADMM

Start with some initial choice of λ (by λ, we include λ<sub>t</sub> corresponding to each time step)
 Assign τ ← arg min<sub>τ</sub> L(τ, θ, λ).
 Assign θ ← arg min<sub>θ</sub> L(τ, θ, λ).
 Compute dg/dλ = dL/dλ (τ, θ, λ). Take a gradient step λ ← λ + α dg/dλ
 Repeat steps 2-4.

Guided Policy Search - Optimization

$$\mathcal{L}( au, heta,\lambda)=c( au)+\sum_{t=1}^T\lambda_t(\pi_ heta(x_t)-u_t)$$

Standard optimization problem Solve it using ADMM

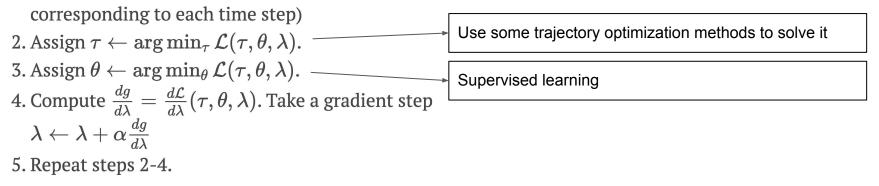
Start with some initial choice of λ (by λ, we include λ<sub>t</sub> corresponding to each time step)
 Assign τ ← arg min<sub>τ</sub> L(τ, θ, λ).
 Use some trajectory optimization methods to solve it
 Assign θ ← arg min<sub>θ</sub> L(τ, θ, λ).
 Compute dg/dλ = dL/dλ(τ, θ, λ). Take a gradient step λ ← λ + α dg/dλ
 Repeat steps 2-4.

Guided Policy Search - Optimization

$$\mathcal{L}( au, heta,\lambda)=c( au)+\sum_{t=1}^T\lambda_t(\pi_ heta(x_t)-u_t)$$

Standard optimization problem Solve it using ADMM

1. Start with some initial choice of  $\lambda$  (by  $\lambda$ , we include  $\lambda_t$ 



Guided Policy Search

$$\mathcal{L}( au, heta,\lambda) = c( au) + \sum_{t=1}^T \lambda_t(\pi_ heta(x_t) - u_t)$$

1. Start with some initial choice of  $\lambda$  (by  $\lambda$ , we include  $\lambda_t$  corresponding to each time step)

2. Assign  $\tau \leftarrow \arg \min_{\tau} \mathcal{L}(\tau, \theta, \lambda)$ .

3. Assign  $\theta \leftarrow \arg \min_{\theta} \mathcal{L}(\tau, \theta, \lambda)$ .

4. Compute  $\frac{dg}{d\lambda} = \frac{d\mathcal{L}}{d\lambda}(\tau, \theta, \lambda)$ . Take a gradient step

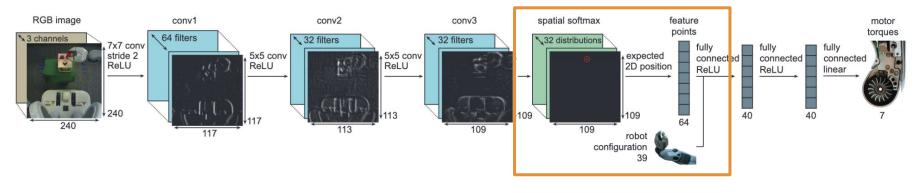
$$\lambda \leftarrow \lambda + \alpha \frac{1}{d\lambda}$$

5. Repeat steps 2-4.

#### Recap:

- Each trajectory-centric teacher only needs to solve the task from a single initial state → make the problem easier
- The policy is trained with
   supervised learning → good generalization
- Iterative adaptation of teacher
   trajectories & final policy → the
   teacher does not take actions that
   the final policy cannot reproduce

#### **Visuomotor Policy Architecture**



$$s_{cij} = e^{a_{cij}} / \sum_{i'j'} e^{a_{ci'j'}}$$

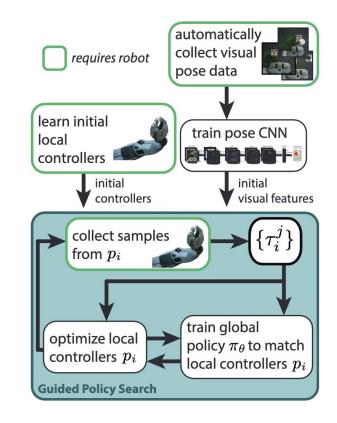
$$f_{cx} = \sum_{ij} s_{cij} x_{ij}$$

$$f_{cy} = \sum_{ij} s_{cij} y_{ij}$$

- Spatial softmax  $\rightarrow$  soft version of max pooling
- Get the feature points
- Learns the spatial information better

# Training procedural

- Pretraining convolutional layers
- Pretraining local controller
- End-to-end guided policy search



# Method

• Algorithm

Target:

$$\min_{p,\pi_{\theta}} E_p[\ell(\tau)] \text{ s.t. } p(\mathbf{u}_t | \mathbf{x}_t) = \pi_{\theta}(\mathbf{u}_t | \mathbf{x}_t) \ \forall \mathbf{x}_t, \mathbf{u}_t, t,$$

$$\ell(\tau) = \sum_{t=1}^{T} \ell(\mathbf{x}_t, \mathbf{u}_t)$$

$$\begin{split} \min_{p,\pi_{\theta}} E_{p}[\ell(\tau)] \text{ s.t. } p(\mathbf{u}_{t}|\mathbf{x}_{t}) = \pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t}) \ \forall \mathbf{x}_{t}, \mathbf{u}_{t}, t, \\ \\ \mathsf{Method} \\ \ell(\tau) = \sum_{t=1}^{T} \ell(\mathbf{x}_{t}, \mathbf{u}_{t}) \\ \bullet \text{ Algorithm} \\ \bullet \text{ Algorithm} \\ \epsilon(\theta, p) = \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\ell(\mathbf{x}_{t},\mathbf{u}_{t})] + E_{p(\mathbf{x}_{t})\pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t})}[\lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] - E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] + \nu_{t}\phi_{t}^{\theta}(\theta, p) \\ p(\theta, \theta) = \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\ell(\mathbf{x}_{t},\mathbf{u}_{t})] + E_{p(\mathbf{x}_{t})\pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t})}[\lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] - E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] + \nu_{t}\phi_{t}^{\theta}(\theta, p) \\ p(\theta, \theta) = \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\ell(\mathbf{x}_{t},\mathbf{u}_{t})] + E_{p(\mathbf{x}_{t})\pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t})}[\lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] - E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] + \nu_{t}\phi_{t}^{\theta}(\theta, p) \\ p(\theta, \theta) = E_{p(\mathbf{x}_{t})}[D_{\mathrm{KL}}(\theta(\mathbf{u}_{t}|\mathbf{x}_{t}))] \\ \theta^{b}_{t}(\theta, p) = E_{p(\mathbf{x}_{t})}[D_{\mathrm{KL}}(\pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t}))] \|p(\mathbf{u}_{t}|\mathbf{x}_{t})]. \\ \theta \leftarrow \arg\min_{\theta} \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t}}] + \mu_{t}\phi_{t}^{\theta}(\theta, p) \\ p \leftarrow \arg\min_{p} \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\ell(\mathbf{x}_{t},\mathbf{u}_{t}] - \lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] + \nu_{t}\phi_{t}^{\theta}(p, \theta) \\ p \leftarrow \arg\min_{p} \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})}[\ell(\mathbf{x}_{t},\mathbf{u}_{t}) - \lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] + \nu_{t}\phi_{t}^{\theta}(p, \theta) \\ \lambda_{\mathbf{x}_{t},\mathbf{u}_{t}} \leftarrow \lambda_{\mathbf{x}_{t},\mathbf{u}_{t}} + \alpha\nu t(\pi(\theta(\mathbf{u}_{t}|\mathbf{x}_{t}))p(\mathbf{x}_{t}) - p(\mathbf{u}_{t}|\mathbf{x}_{t})p(\mathbf{x}_{t})). \end{split}$$

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#### Method

Algorithm  $\theta \leftarrow \arg\min_{\theta} \sum_{t \in I} E_{p(\mathbf{x}_t)\pi_{\theta}(\mathbf{u}_t|\mathbf{x}_t)}[\lambda_{\mathbf{x}_t,\mathbf{u}_t}] + \nu_t \phi_t^{\theta}(\theta,p)$  $p \leftarrow \arg\min_{p} \sum_{t=1} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})} [\ell(\mathbf{x}_{t},\mathbf{u}_{t}) - \lambda_{\mathbf{x}_{t},\mathbf{u}_{t}}] + \nu_{t} \phi_{t}^{p}(p,\theta)$  $\lambda_{\mathbf{x}_t,\mathbf{u}_t} \leftarrow \lambda_{\mathbf{x}_t,\mathbf{u}_t} + \alpha \nu_t (\pi_\theta(\mathbf{u}_t|\mathbf{x}_t)p(\mathbf{x}_t) - p(\mathbf{u}_t|\mathbf{x}_t)p(\mathbf{x}_t)).$  $\theta \leftarrow \arg\min_{\theta} \sum_{t \in T} E_{p(\mathbf{x}_t)\pi_{\theta}(\mathbf{u}_t | \mathbf{x}_t)} [\mathbf{u}_t^{\mathrm{T}} \lambda_{\mu t}] + \nu_t \phi_t^{\theta}(\theta, p)$  $p \leftarrow \arg\min_{p} \sum_{t=1}^{T} E_{p(\mathbf{x}_{t},\mathbf{u}_{t})} [\ell(\mathbf{x}_{t},\mathbf{u}_{t}) - \mathbf{u}_{t}^{\mathrm{T}}\lambda_{\mu t}] + \nu_{t}\phi_{t}^{p}(p,\theta)$  $\lambda_{\mu t} \leftarrow \lambda_{\mu t} + \alpha \nu_t (E_{\pi_\theta(\mathbf{u}_t | \mathbf{x}_t) p(\mathbf{x}_t)}[\mathbf{u}_t] - E_{p(\mathbf{u}_t | \mathbf{x}_t) p(\mathbf{x}_t)}[\mathbf{u}_t]),$ 

$$\textbf{Method} \qquad \qquad \mathcal{L}_p(p,\theta) = \sum_{t=1}^T E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\ell(\mathbf{x}_t,\mathbf{u}_t)] + E_{p(\mathbf{x}_t)\pi_\theta(\mathbf{u}_t|\mathbf{x}_t)}[\lambda_{\mathbf{x}_t,\mathbf{u}_t}] - E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\lambda_{\mathbf{x}_t,\mathbf{u}_t}] + \nu_t \phi_t^p(\theta,p), \\ p \leftarrow \arg\min_p \sum_{t=1}^T E_{p(\mathbf{x}_t,\mathbf{u}_t)}[\ell(\mathbf{x}_t,\mathbf{u}_t) - \mathbf{u}_t^T \lambda_{\mu t}] + \nu_t \phi_t^p(p,\theta)$$

• Trajectory optimization under unknown dynamics

$$p(\mathbf{u}_t|\mathbf{x}_t) = \mathcal{N}(\mathbf{K}_t\mathbf{x}_t + \mathbf{k}_t, \mathbf{C}_t) \qquad p(\mathbf{x}_{t+1}|\mathbf{x}_t, \mathbf{u}_t) = \mathcal{N}(f_{\mathbf{x}t}\mathbf{x}_t + f_{\mathbf{u}t}\mathbf{u}_t + f_{ct}, \mathbf{F}_t).$$

$$\min_{p(\tau)\in\mathcal{N}(\tau)} \mathcal{L}_p(p,\theta) \text{ s.t. } D_{\mathrm{KL}}(p(\tau)\|\hat{p}(\tau)) \leq \epsilon.$$

$$\textbf{Method} \quad \begin{aligned} \mathcal{L}_{\theta}(\theta, p) &= \sum_{t=1}^{T} E_{p(\mathbf{x}_{t}, \mathbf{u}_{t})} [\ell(\mathbf{x}_{t}, \mathbf{u}_{t})] + E_{p(\mathbf{x}_{t})\pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t})} [\lambda_{\mathbf{x}_{t}, \mathbf{u}_{t}}] - E_{p(\mathbf{x}_{t}, \mathbf{u}_{t})} [\lambda_{\mathbf{x}_{t}, \mathbf{u}_{t}}] + \nu_{t} \phi_{t}^{\theta}(\theta, p) \\ \theta &\leftarrow \arg \min_{\theta} \sum_{t=1}^{T} E_{p(\mathbf{x}_{t})\pi_{\theta}(\mathbf{u}_{t}|\mathbf{x}_{t})} [\mathbf{u}_{t}^{\mathrm{T}} \lambda_{\mu t}] + \nu_{t} \phi_{t}^{\theta}(\theta, p) \end{aligned}$$

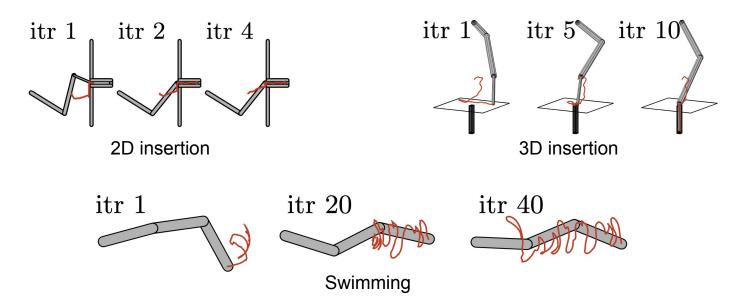
• Supervised policy optimization

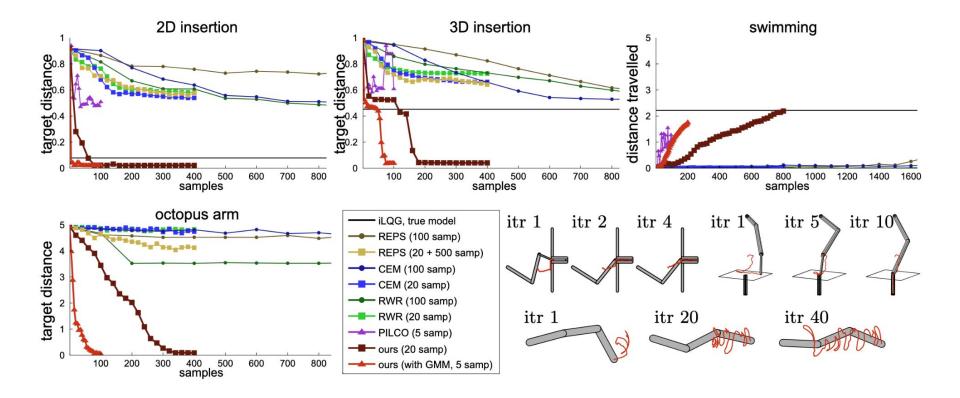
$$\begin{aligned} \mathcal{L}_{\theta}(\theta, p) = & \frac{1}{2N} \sum_{i=1}^{N} \sum_{t=1}^{T} E_{p_i(\mathbf{x}_t, \mathbf{o}_t)} \left[ \operatorname{tr}[\mathbf{C}_{ti}^{-1} \Sigma^{\pi}(\mathbf{o}_t)] - \log |\Sigma^{\pi}(\mathbf{o}_t)| \right. \\ & \left. + (\mu^{\pi}(\mathbf{o}_t) - \mu_{ti}^p(\mathbf{x}_t)) \mathbf{C}_{ti}^{-1} (\mu^{\pi}(\mathbf{o}_t) - \mu_{ti}^p(\mathbf{x}_t)) + 2\lambda_{\mu t}^{\mathrm{T}} \mu^{\pi}(\mathbf{o}_t) \right], \end{aligned}$$

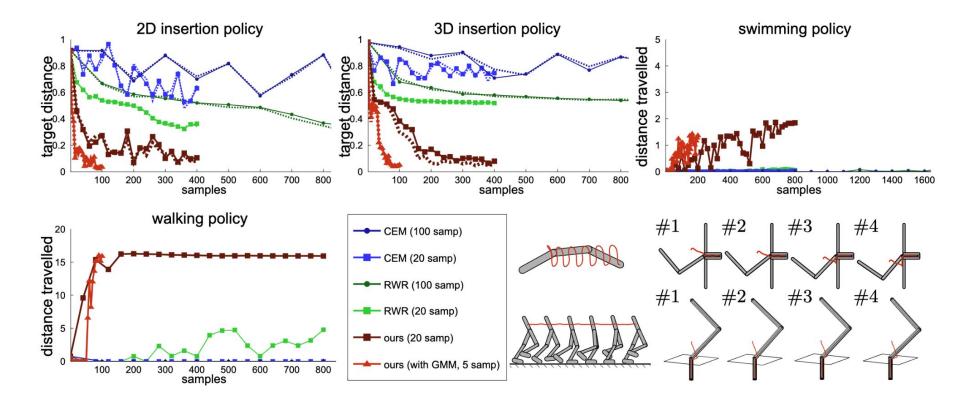
 $\pi_{ heta}(\mathbf{u}_t | \mathbf{o}_t) = \mathcal{N}(\mu^{\pi}(\mathbf{o}_t), \Sigma^{\pi}(\mathbf{o}_t))$ 

- How does the guided policy search algorithm compare to other policy search methods for training complex, high-dimensional policies, such as neural networks?
- Does our trajectory optimization algorithm work on a real robotic platform with unknown dynamics, for a range of different tasks?
- How does our spatial softmax architecture compare to other, more standard convolutional neural network architectures?
- Does training the perception and control systems in a visuomotor policy jointly end-to-end provide better performance than training each component separately?

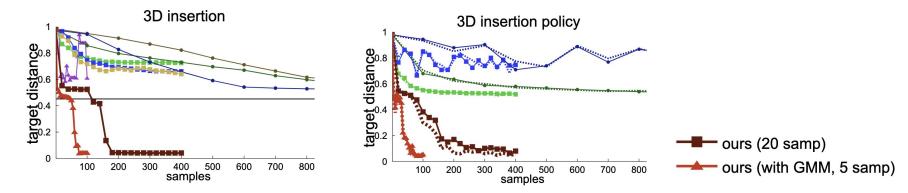
 How does the guided policy search algorithm compare to other policy search methods for training complex, high-dimensional policies, such as neural networks?







- How does the guided policy search algorithm compare to other policy search methods for training complex, high-dimensional policies, such as neural networks?
  - Compare with methods that do not use vision, but use system states
  - GPS is more sample efficient
  - Better generalization in testing





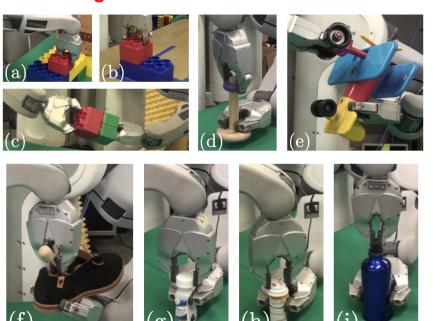
• Does our trajectory optimization algorithm work on a real robotic platform with unknown dynamics, for a range of different tasks?



- Sample efficient (20-25 samples)
- Robustness



- Does our trajectory optimization algorithm work on a real robotic platform with unknown dynamics, for a range of different tasks?
  - Sample efficient (20-25 samples)
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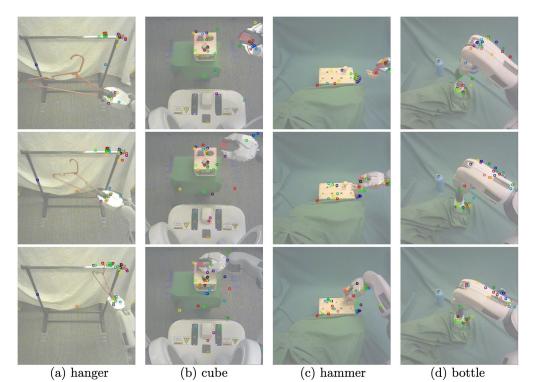


• How does our spatial softmax architecture compare to other, more standard convolutional neural network architectures?

network architecture	test error (cm)
softmax + feature points (ours)	$\textbf{1.30} \pm \textbf{0.73}$
softmax + fully connected layer	$2.59 \pm 1.19$
fully connected layer	$4.75 \pm 2.29$
max-pooling + fully connected	$3.71 \pm 1.73$

Performance on Object Pose Estimation Pretraining Task

• Visualization of feature points



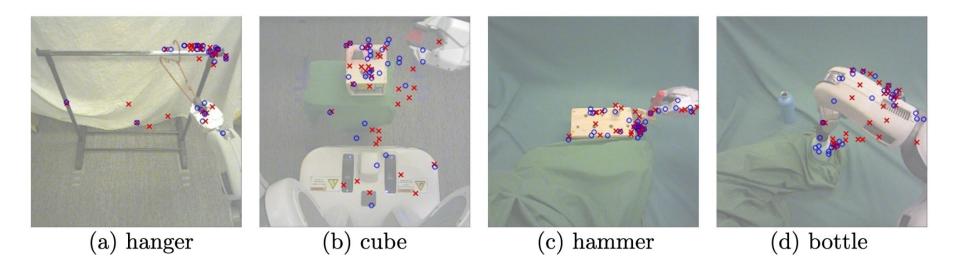
 Does training the perception and control systems in a visuomotor policy jointly end-to-end provide better performance than training each component separately?

#### Baselines:

train the vision layers in advance, then train the policy

coat hanger	training $(18)$	spatial test $(24)$	visual test $(18)$
end-to-end	100%	100%	100%
pose features	88.9%	87.5%	83.3%
pose prediction	55.6%	58.3%	66.7%
shape cube	training $(27)$	spatial test (36)	visual test $(40)$
end-to-end	96.3%	91.7%	87.5%
pose features	70.4%	83.3%	40%
pose prediction	0%	0%	n/a
toy hammer	training $(45)$	spatial test $(60)$	visual test $(60)$
end-to-end	91.1%	86.7%	78.3%
pose features	62.2%	75.0%	53.3%
pose prediction	8.9%	18.3%	n/a
bottle cap	training $(27)$	spatial test $(12)$	visual test $(40)$
end-to-end	88.9%	83.3%	62.5%
pose features	55.6%	58.3%	27.5%

Success rates on training positions, on novel test positions, and in the presence of visual distractors. The number of trials per test is shown in parentheses.



- What are the drawbacks/limitations for this method?

• Needs Full-state observations during training

- Needs Full-state observations during training
- Dependent on hand-crafted rewards

- Needs Full-state observations during training
- Dependent on hand-crafted rewards
- Relying on the ability of Trajectory Optimization Method (teachers) to discover good trajectories

#### Questions?